

Short Course on
**GEOMEMBRANES AND COMPOSITE LINERS
IN LANDFILLS AND MINING:
MOVING FORWARD**

Sunday 17 Sept. 2023

2. Leakage through liners

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Geomembranes

- **Essentially impermeable –**
 - **unless they have holes**



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Short-term processes that can increase fluid ingress or egress

- Greatest short-term risk is due to hole formation:
 - During construction - minimized by good design, CQC/CQA
 - Due to activities above completed liner
 - Possibly due to animals (e.g., rodents, bears)
 - both minimized by good design and site-use restrictions
 - Caused by excessive differential settlement
 - Due to nature of materials above/below GMB and applied pressures

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Construction-related holes in GMB

- 2.5 – 10 holes/ha typical design value
- 3 holes/ha after installation*
- 12 holes/ha after placement of drainage layer*
- 5 holes/ha assumed in presentation
- Median equivalent radius – 5.6mm (typical)

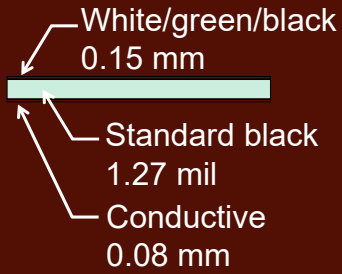


* Nosko & Touze-Foltz (2000)

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Spark testing

1.5mm Conductive
white GMB



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Holes in Geomembranes (GMBs)

To minimize holes in
geomembranes (GMBs) need:

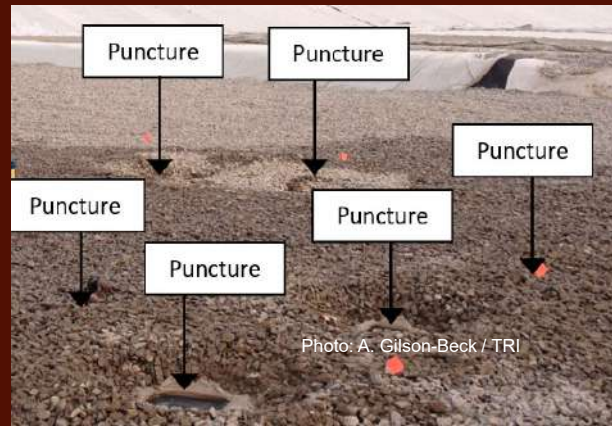
- High-quality CQA ,and
- Leak detection
 - Puddle method: exposed GMB
detect holes ≥ 1 mm



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Geomembranes (GMBs)

- Holes in geomembranes occur
 - during installation (mostly eliminated by good CQA)
 - with placement of cover soil over the GMB
there can be >20 holes/ha (Giroud 2017)



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Bituminous Geomembranes (BGMs)

(Bremner et al. 2016)

- 230,600 m² of BGM + soil used to cover tailings and waste rock in Canada
- 39 holes/ha (5 mm to 150 mm diameter) in 2011
- 18.4 holes/ha in 2012



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Holes in Geomembranes (GMBs)

Locating holes in geomembranes (GMBs) need:

- High-quality CQA ,and
- Leak detection
 - Puddle method: exposed GMB detect holes ≥ 1 mm
- Double Dipole Survey:
 - Water covered GMB
 - Soil covered GMB detect holes ≥ 6 mm under 0.6 m soil



(Photo: TRI)

[9]

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Source: Darilek and Laine (2007)

Leak detection survey

- electrically conductive medium above and below GMB
 - wet gravel or geotextile over GMB
- induce voltage difference between top and bottom
- passed electrodes over top to measure electrical potential
- anomalies in electrical potential indicate holes in GMB
 - caused by flow of current along conductive path through the hole

ASTM D7002 or D7007

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Geomembranes (GMBs)

- Holes in geomembranes occur
 - during installation (mostly eliminated by good CQA)
 - with placement of cover soil (may be detected & eliminated)
 - **post-construction (shorter- and longer-term))**



**Short-term
puncture**

**Longer-term
stress crack**



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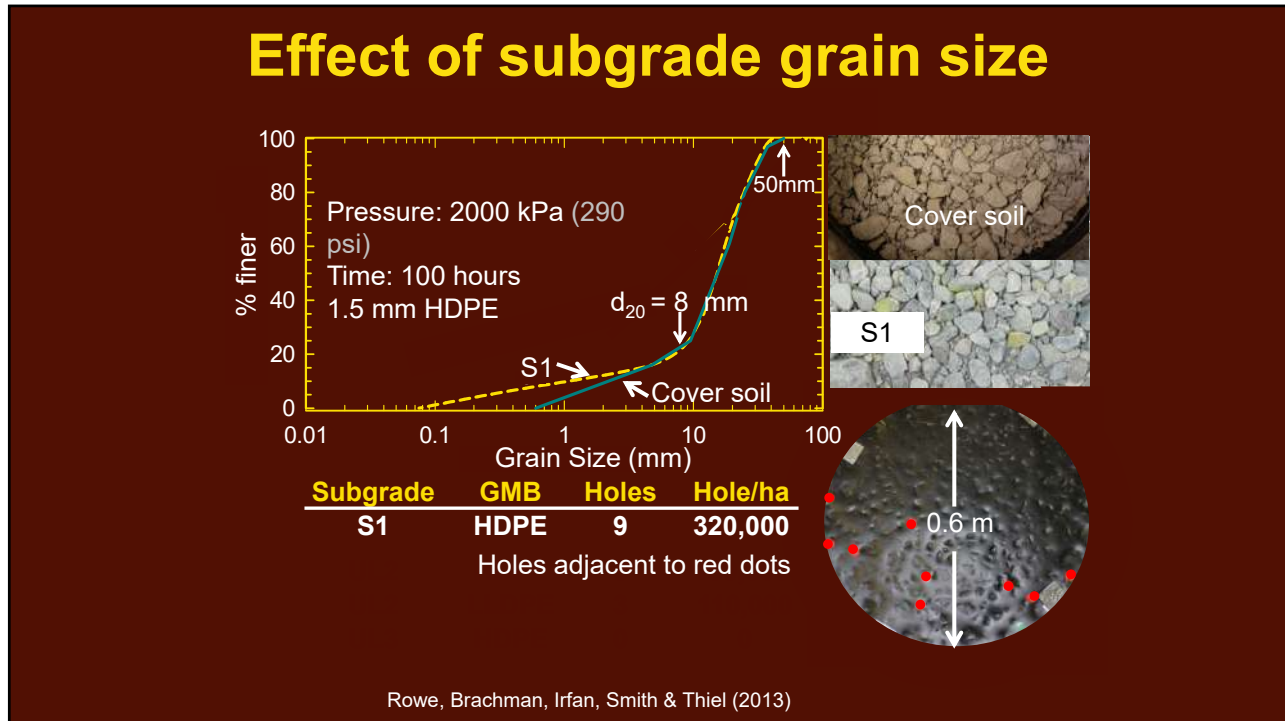
Puncture and excessive strain due to applied pressures

- Short-term puncture
- Strains generate longer-term failure
- Vertical pressure ≤ 3000 kPa

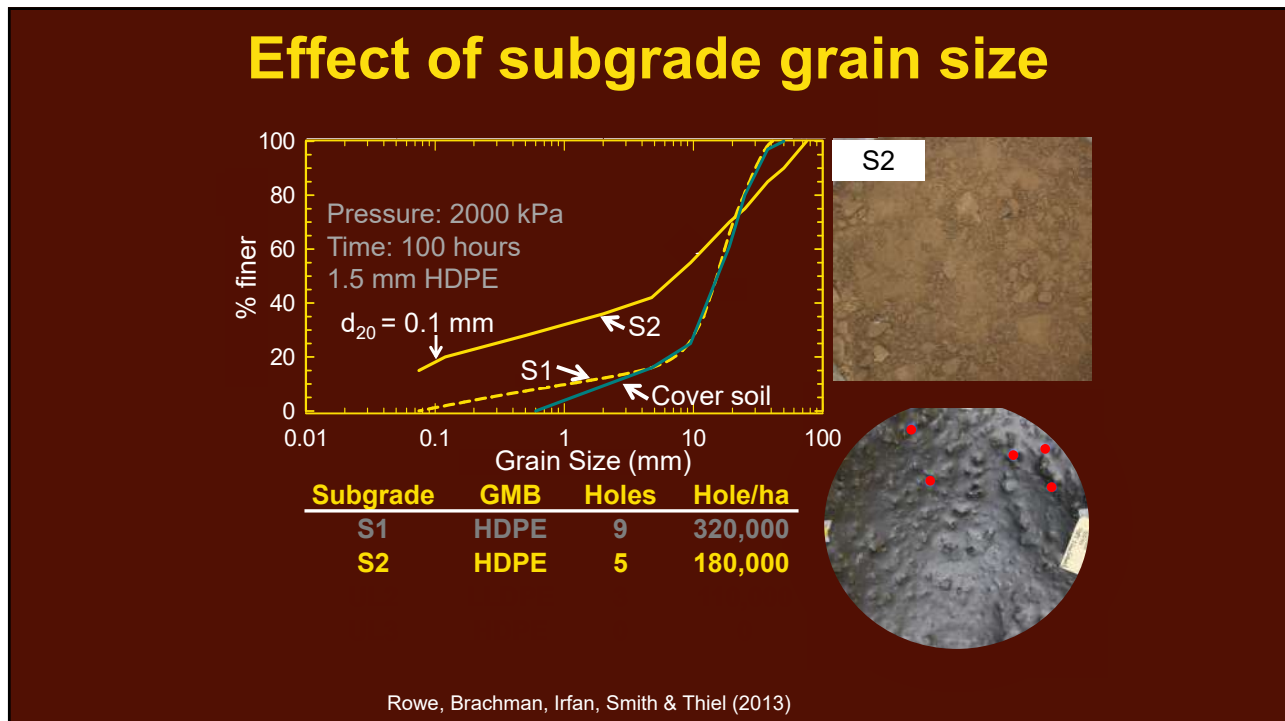
Geosynthetic liner
longevity simulator
GLLS



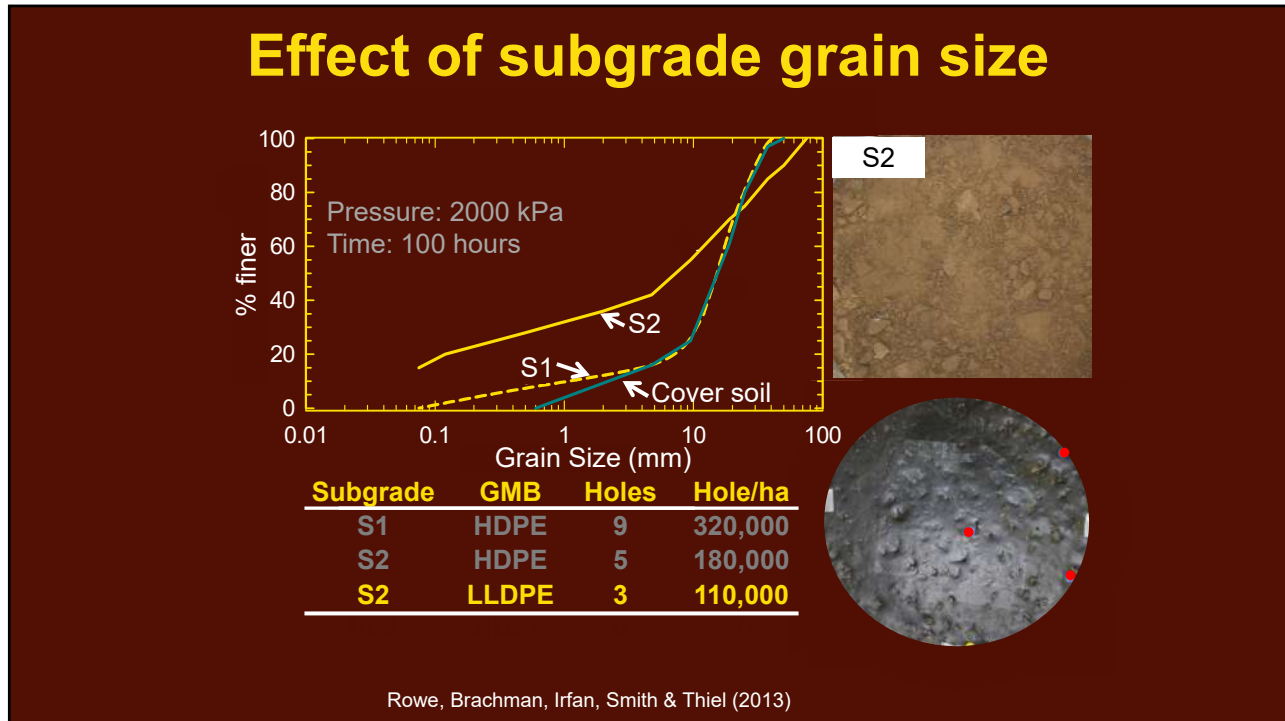
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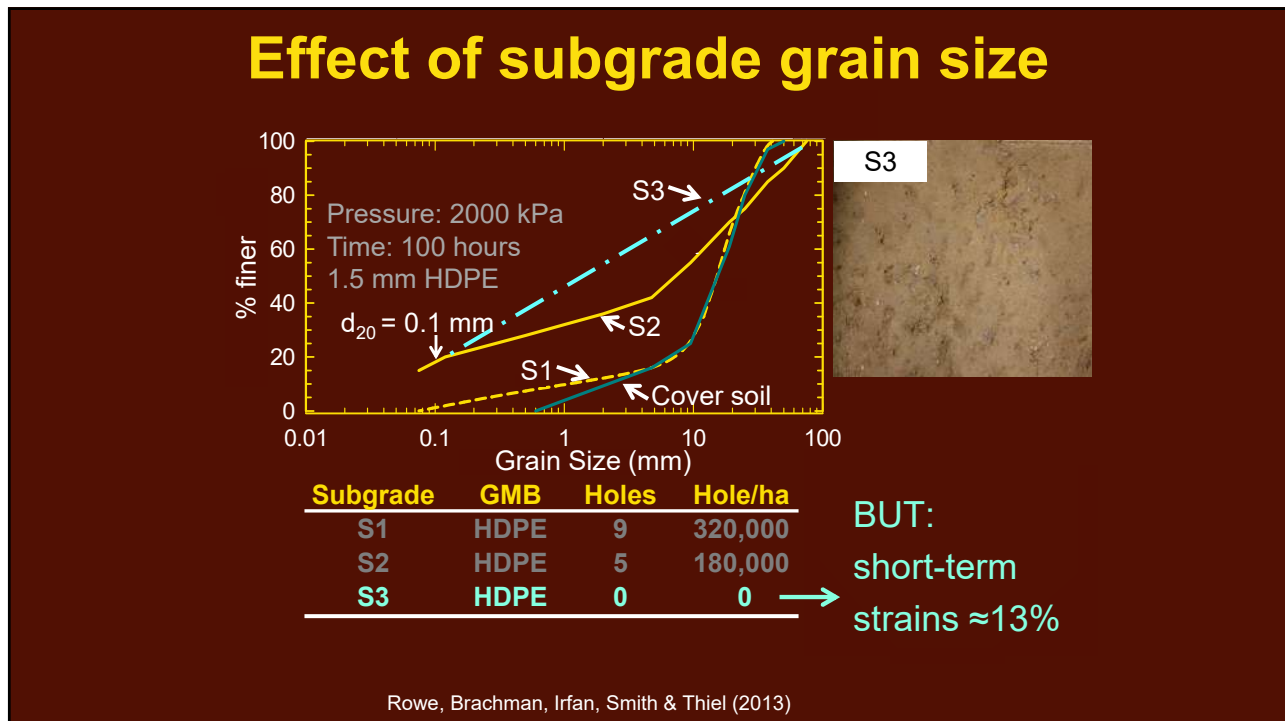
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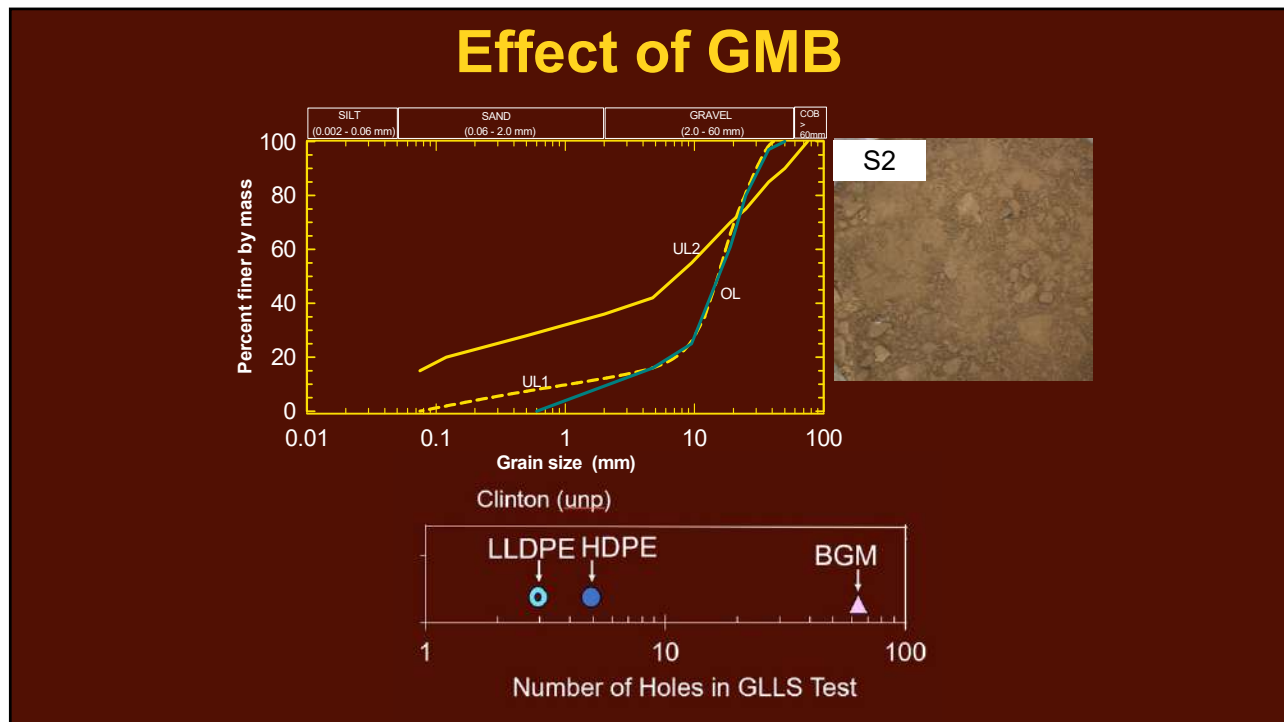
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Post-construction hole summary

- Isolated stones in finer grained subgrade may be worse than packed gravel
- Puncture likely when with a coarse gap graded cover soil and subgrade
- Even if no puncture with coarse cover soil (and finer subgrade), short-term strains $\approx 13\%$
- **Shape of the grading curve** of soil adjacent to GMB has a much greater effect on **puncture and strains** than the maximum particle size

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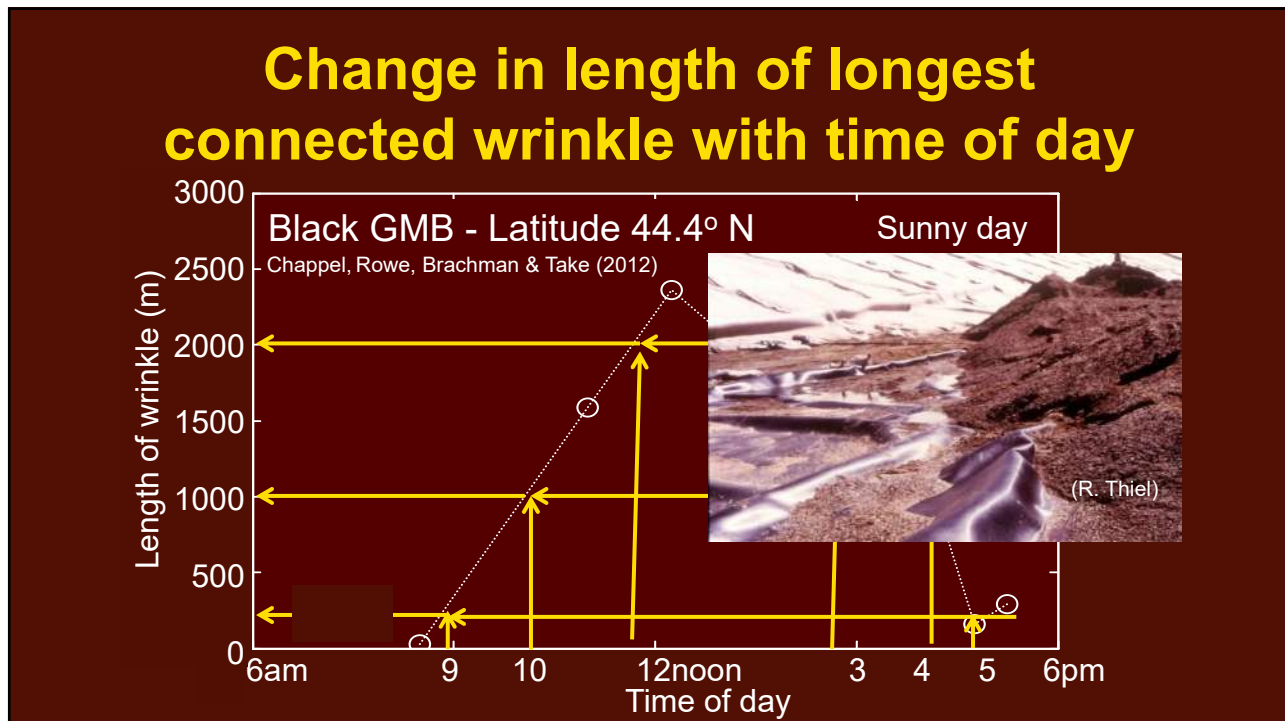
GMB thermally induced wrinkles/waves

GMB $T \approx 45^\circ\text{C}$
(110 °F)

SAME GMB with wrinkles a few hours later when ambient $T = 17^\circ\text{C}$
(63 °F)

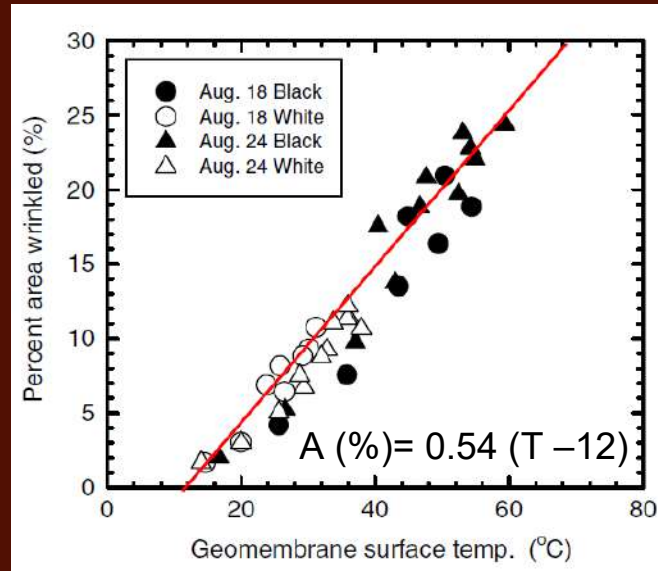
Rowe, Chappel, Brachman & Take (2012)

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Effect of GMB Colour on Wrinkles



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Covered Wrinkles get Holes

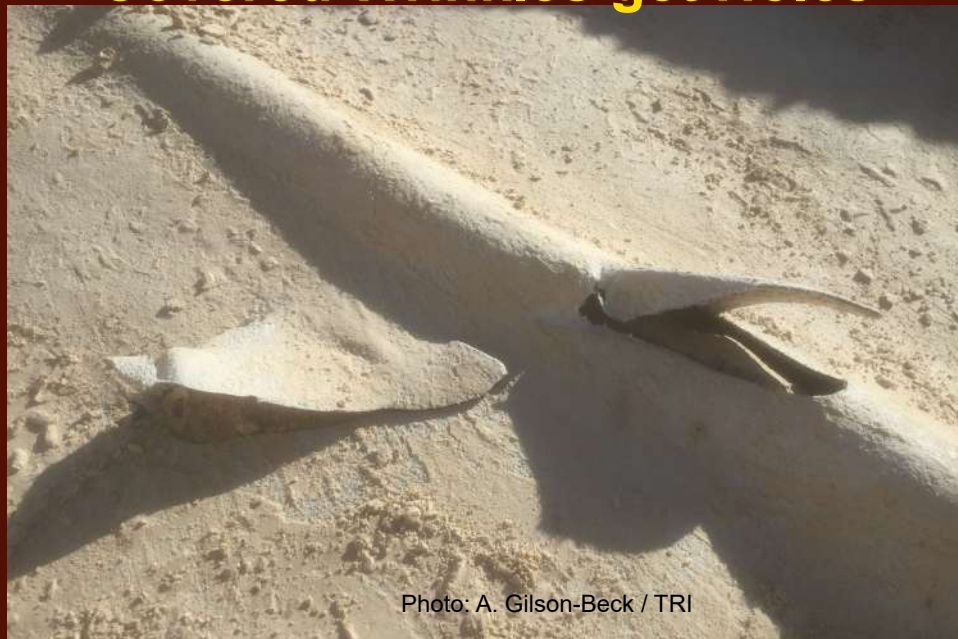

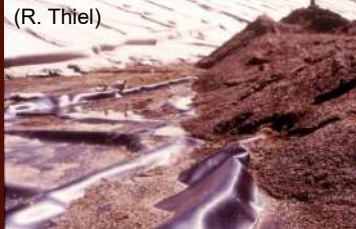


Photo: A. Gilson-Beck / TRI

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Probability of a holed-wrinkle (Good CQA but no ELLS)

	Wrinkle length (m)	Probability (%)	
	≥ 100	70	
	≥ 200	50	
	≥ 500	15	
	≥ 1000	4	

(Based on New York leakage data; Beck 2015) Rowe (2018)

**Message: You will grossly underestimate leakage if
you do not consider holes in wrinkles**

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How to decrease the number of wrinkles in your liner?

- Cover the GMBs early in the morning
- Use white GMB

What are the consequences of having too many wrinkles in your liner?

- Increased leakage
- Stress cracking

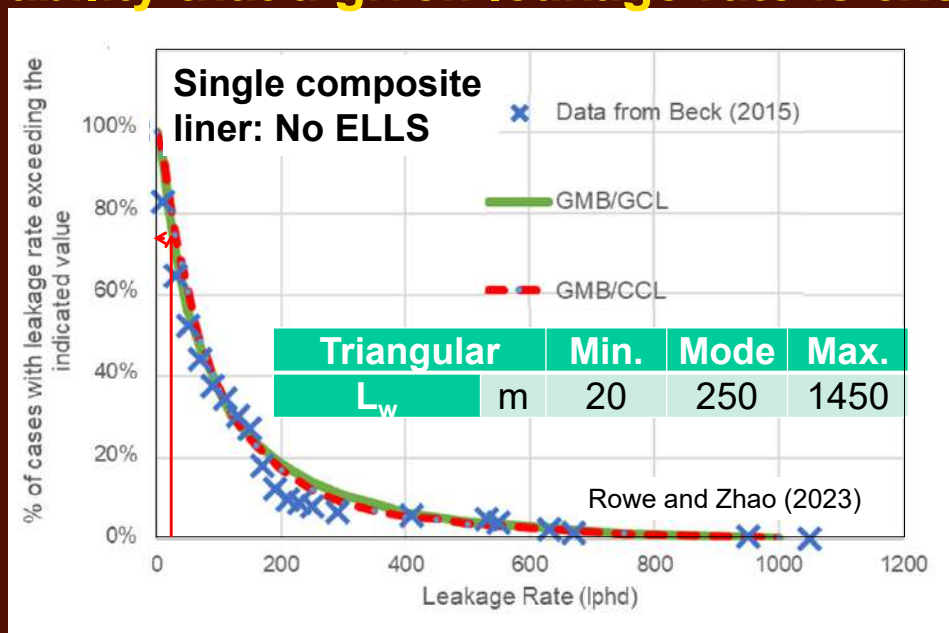
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Warning

- The material presented is not complete in and of itself; it is intended only to provide direction and examples. Examine published sources for more complete information.
- The reader is responsible for assessing the relevance and usefulness for any project
- Typical ranges are for typical conditions - many non-typical conditions exist.
- Average or typical values may have 50% above and 50% below

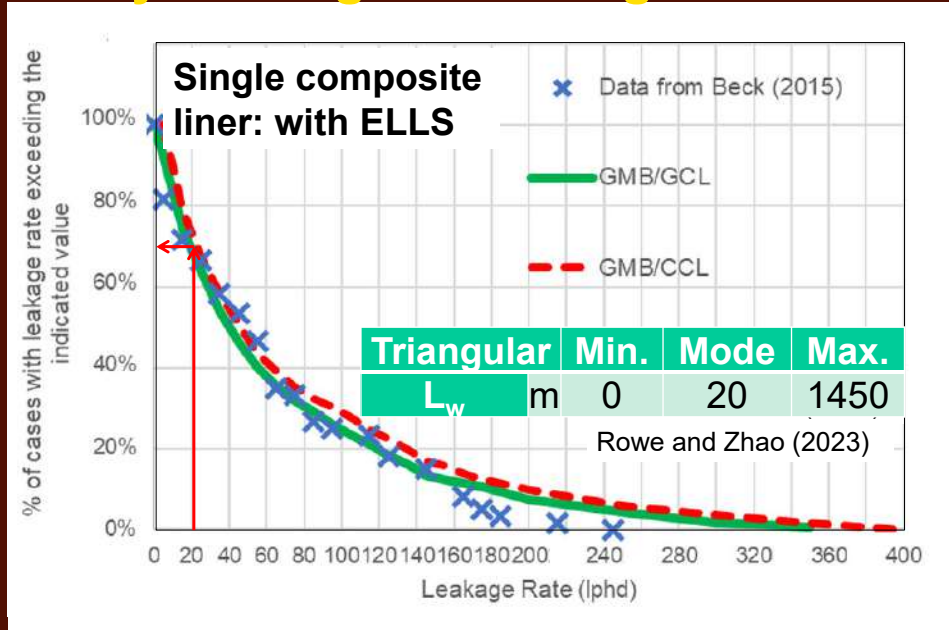
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Probability that a given leakage rate is exceeded



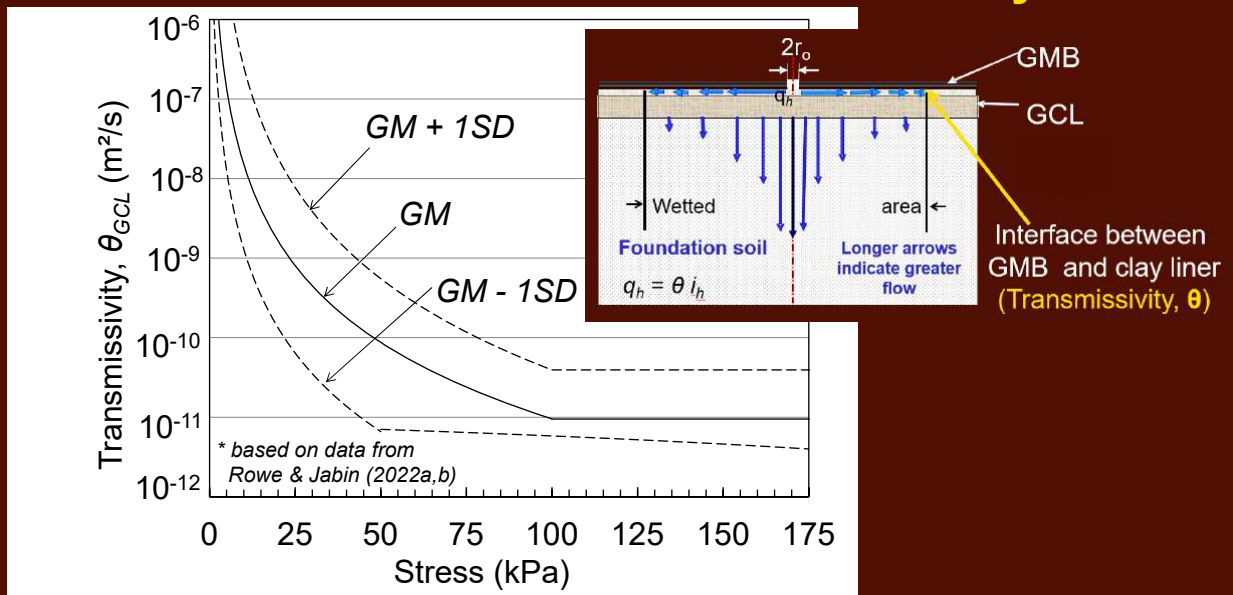
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Probability that a given leakage rate is exceeded



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GMB/GCL Interface Transmissivity



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Example liner parameters	$\sigma_{va} < 5 \text{ kPa}$ <i>Pond</i> ¹	$\sigma_{va} \sim 15 \text{ kPa}$ <i>Cover</i> ²	$\sigma_{va} \geq 150 \text{ kPa}$ <i>bottom liner</i> ³
Head on liner, h (m)	5	0.15	0.2
Hole area, a (mm ²)	100	100	100
Holed wrinkle length, L_w (no ELLS) (m)	530	530	530
Holed wrinkle length, L_w (ELLS) (m)	430	430	430
Holed wrinkle average width, $2b$ (m)	0.2	0.2	0.1
Liner thickness, GCL, H_{GCL} (m)	0.015	0.01	0.007
Hydraulic conductivity below wrinkle, k_{bGCL} (m/s)	2×10^{-10}	6×10^{-8} to 2×10^{-10}	6×10^{-8} to 2×10^{-10}
Hydraulic conductivity below wrinkle, k_{aGCL} (m/s)	5×10^{-11}	2×10^{-10}	3×10^{-11}
Hydraulic conductivity MGCL, k_{GCL} (m/s)	5×10^{-11}	5×10^{-11}	5×10^{-11}
GMB/GCL interface transmissivity, θ_{GCL} (m ² /s)	1×10^{-8}	3×10^{-9}	3×10^{-11}
Liner thickness, CCL, H_{CCL} (m)	0.6	0.6	0.6
Hydraulic conductivity below wrinkle, k_{CCL} (m/s)	1×10^{-9}	1×10^{-8}	2×10^{-10}
GMB/GCL interface transmissivity, θ_{CCL} (m ² /s)	1×10^{-6}	1×10^{-7}	2×10^{-9}

¹ Submerged and about 0.3 m cover soil; ² About 1 m cover soil; ³ MSW Landfill about 0.3 m gravel drainage layer.

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Leakage through a clay liner alone

1. Darcy's law $Q = A k h/H$ $A = \text{area (m}^2\text{)}$, $h = \text{head (m)}$, $H = \text{thickness (m)}$

	$\sigma_{va} < 5 \text{ kPa}$ <i>Pond</i> ¹	$\sigma_{va} \sim 15 \text{ kPa}$ <i>Cover</i> ²	$\sigma_{va} \geq 150 \text{ kPa}$ <i>bottom liner</i> ³
Head on liner, h (m)	5	0.15	0.2
Liner thickness, GCL, H_{GCL} (m)	0.015	0.01	0.007 m
Hydraulic conductivity normal GCL, k_{GCL} (m/s)	2×10^{-10}	6×10^{-8} m/s	2×10^{-10} m/s
Leakage with Darcy Equation (lphd)	57,800	829,000	5,100
Hydraulic conductivity MGCL, k_{GCL}	5×10^{-11} m/s	5×10^{-11} m/s	5×10^{-11} m/s
Leakage with Darcy Equation (lphd)	14,400	700	1300
Liner thickness, CCL, H_{CCL}	0.6 m	0.6 m	0.6 m
Hydraulic conductivity k_{CCL}	1×10^{-9} m/s	1×10^{-8} m/s	2×10^{-10} m/s
Leakage with Darcy Equation (lphd)	8,000	11,000	230

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Leakage through a geomembrane defect

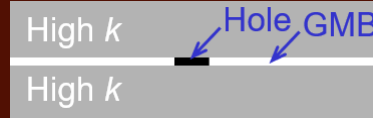
1. Darcy's law $Q = A k h/H$ $A = \text{area (m}^2\text{)}$, $h = \text{head (m)}$, $H = \text{thickness (m)}$

2. Bernoulli's equation $a = \text{area of hole (m}^2\text{)}$

$$Q = 2.6 a \sqrt{h}$$

$h = \text{head (m)}$

$Q = \text{leakage (m}^3\text{/s)}$



$2r_o$ $a = \pi r_o^2$

	$\sigma_{va} < 5 \text{ kPa}$ <i>Pond</i> ¹	$\sigma_{va} \sim 15 \text{ kPa}$ <i>Cover</i> ²	$\sigma_{va} \geq 150 \text{ kPa}$ <i>bottom liner</i> ³
Head on liner, h (m)	5	0.15	0.2
Leakage with Darcy Equation, MGCL alone (lphd)	14,400	700	1,300
Leakage with Darcy Equation, CCL alone (lphd)	8,000	11,000	230
Hole area, a (mm ²)	100	100	100
Leakage from Bernoulli's Eq. Q (lphd)	51,000	8,900	10,300

Maximum leakage possible through this hole in a wrinkle

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Leakage through a geomembrane defect

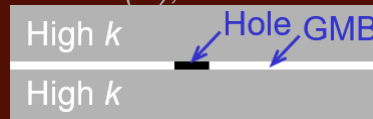
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2. Bernoulli's equation $a = \text{area of hole (m}^2\text{)}$

$$Q = 2.6 a \sqrt{h}$$

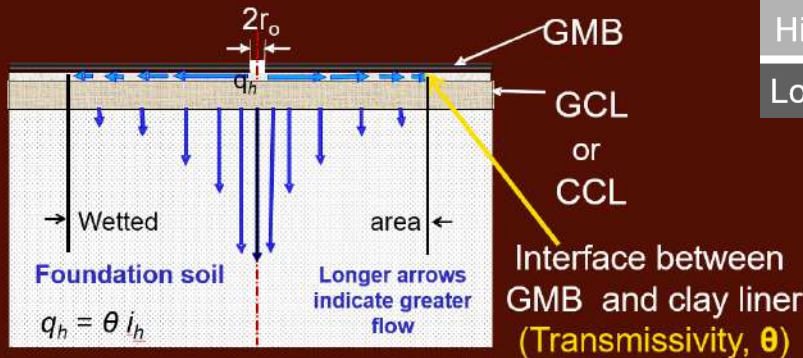
$h = \text{head (m)}$

$Q = \text{leakage (m}^3\text{/s)}$



$2r_o$ $a = \pi r_o^2$

3. Rowe (1998) equation if hole in direct contact



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Rowe (1998) equation if hole in direct contact

Spread sheet: Data > what-if analysis>goal seek (dh/dr, 0, R)

Input	Input	Input	Input	Input	\$O	Output	\$AA
Hole radius r_o (m)	Permeability of liner k_L (m/s)	Thickness of Liner H_L (m)	h_w (m)	θ (m ² /s)	Wetted radius R (m)	$Q_{\text{calculated}}$ (L/d)	dh/dr
0.005642	5.00E-11	0.015	5	1.00E-08	7.544	4.667	0.00
0.005642	2.00E-10	0.015	5	1.00E-08	3.804	5.268	0.00
0.005642	2.00E-10	0.01	0.15	3.00E-09	0.808	0.059	0.00
0.005642	6.00E-08	0.01	0.15	3.00E-09	0.065	0.166	0.00
0.005642	3.00E-11	0.007	0.2	3.00E-11	0.243	0.001	0.00
0.005642	3.00E-11	0.007	0.2	3.00E-11	0.243	0.001	0.00
0.005642	1.00E-09	0.6	5	1.00E-06	31.452	560.33	0.00
0.005642	1.00E-08	0.6	0.15	1.00E-07	0.814	3.60	0.00
0.005642	2.00E-10	0.6	0.2	2.00E-09	0.919	0.092	0.00

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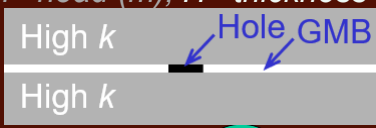
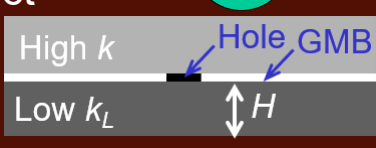
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Head on liner, h (m)	5	0.15	0.2
Leakage with Darcy Equation, MGCL alone (lphd)	14,400	700	1,300
Hole area, a (mm ²)	100	100	100
Leakage from Bernoulli's Eq. Q (lphd)	51,000	8,900	10,300
Liner thickness, GCL , H_{GCL} (m)	0.015	0.01	0.007
Hydraulic conductivity, k_{GCL} (m/s)	2×10^{-10}	6×10^{-8}	3×10^{-11}
GMB/GCL interface transmissivity, θ_{GCL} (m ² /s)	1×10^{-8}	3×10^{-9}	3×10^{-11}
Leakage with Rowe (1998) Equation for DC (lphd)	≤ 5.3	< 0.2	0.001
Liner thickness, CCL , H_{GCL} (m)	0.6	0.6	0.6
Hydraulic conductivity below wrinkle, k_{CCL} (m/s)	1×10^{-9}	1×10^{-8}	2×10^{-10}
GMB/GCL interface transmissivity, θ_{CCL} (m ² /s)	1×10^{-6}	1×10^{-7}	2×10^{-9}
Leakage with Rowe (1998) Equation (lphd)	560	3.6	0.09

¹ Submerged and about 0.3 m cover soil; ² About 1 m cover soil; ³ MSW Landfill about 0.3 m gravel drainage layer.

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Leakage through a geomembrane defect

- Darcy's law $Q = A k h/H$ A =area (m^2), h =head (m), H = thickness (m)
- Bernoulli's equation a = area of hole (m^2)
 $Q = 2.6 a \sqrt{h}$ h = head (m)
 Q = leakage (m^3/s)
- Giroud's (1997) if hole in direct contact
 $Q = C_q [1 + 0.1(h/H)^{0.95}] a^{0.1} h^{0.9} k_L^{0.75}$

- Valid within strict limits
- Most misused equation (outside of limits on hole size and head – see Giroud's paper)
- Assumes direct intimate contact

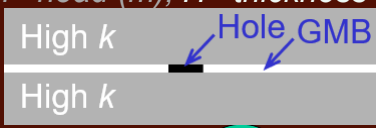
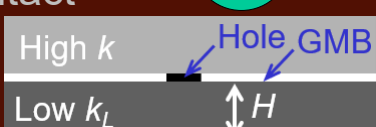
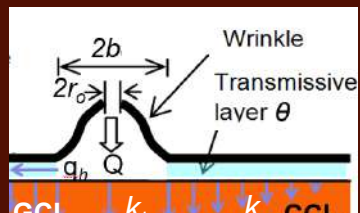
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	$\sigma_{va} < 5 \text{ kPa}$ <i>Pond</i> ¹	$\sigma_{va} \sim 15 \text{ kPa}$ <i>Cover</i> ²	$\sigma_{va} \geq 150 \text{ kPa}$ <i>bottom liner</i> ³
Head on liner, h (m)	5	0.15	0.2
Leakage with Darcy Equation, MGCL alone (lphd)	14,400	700	1300
Leakage with Darcy Equation, CCL alone (lphd)	8,000	11,000	230
Hole area, a (mm^2)	100	100	100
Leakage from Bernoulli's Eq. Q (lphd)	51,000	8,900	10,300
Liner thickness, GCL, H_{GCL} (m)	0.015	0.01	0.007 m
Hydraulic conductivity, k_{GCL} (m/s)	2×10^{-10}	6×10^{-8}	3×10^{-11}
GMB/GCL interface transmissivity, θ_{GCL} (m^2/s)	1×10^{-8}	3×10^{-9}	3×10^{-11}
Leakage with Rowe (1998) DC Eq. (lphd)	≤ 5.3	< 0.2	0.001
Leakage with Giroud (1997) DC Eq. (lphd)	na	14	0.06
Liner thickness, CCL, H_{GCL} (m)	0.6 m	0.6 m	0.6 m
Hydraulic conductivity below wrinkle, k_{CCL} (m/s)	1×10^{-9} m/s	1×10^{-8} m/s	2×10^{-10} m/s
GMB/GCL interface transmissivity, θ_{CCL} (m^2/s)	1×10^{-6} m^2/s	1×10^{-7} m^2/s	2×10^{-9} m^2/s
Leakage with Rowe (1998) DC Eq. (lphd)	560	3.6	0.09
Leakage with Giroud (1997) DC Eq. (lphd)	na	1.6(g)-8.9(p)	0.4(g)

¹ Submerged and about 0.3 m cover soil; ² About 1 m cover soil; ³ MSW Landfill about 0.3 m gravel drainage layer.

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Leakage through a geomembrane defect

- Darcy's law $Q = A k h/H$ $A = \text{area (m}^2\text{)}$, $h = \text{head (m)}$, $H = \text{thickness (m)}$
- Bernoulli's equation $a = \text{area of hole (m}^2\text{)}$
 $Q = 2.6 a \sqrt{h}$ $h = \text{head (m)}$
 $Q = \text{leakage (m}^3\text{/s)}$

- Giroud's equation if hole in direct contact
 $Q = C_q [1 + 0.1(h/H)^{0.95}] a^{0.1} h^{0.9} k_L^{0.75}$

- Rowe's equation if hole in a wrinkle
 $Q = L [2b k_b + 2(k_a H \theta)^{0.5}] h / H$


No ELLS

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Example parameters – GCL	$\sigma_{va} < 5 \text{ kPa}$ Pond ¹	$\sigma_{va} \sim 15 \text{ kPa}$ Cover ²	$\sigma_{va} \geq 150 \text{ kPa}$ bottom liner ³
Head on liner, h (m)	5	0.15	0.2
Hole area, a (mm ²)	100	100	100
Holed wrinkle length, L_w (no ELLS) (m)	530	530	530
Holed wrinkle average width, $2b$ (m)	0.2	0.15	0.1
Leakage from Bernoulli's Eq. Q (lphd)	51,000	8,900	10,300
Liner thickness, GCL, H_{GCL} (m)	0.015	0.01	0.007
Hydraulic conductivity below wrinkle, k_{bGCL} (m/s)	2×10^{-10}	6×10^{-8} to 2×10^{-10}	6×10^{-8} to 2×10^{-10}
Hydraulic conductivity below wrinkle, k_{aGCL} (m/s)	5×10^{-11}	2×10^{-10}	3×10^{-11}
GMB/GCL interface transmissivity, θ_{GCL} (m ² /s)	1×10^{-8}	3×10^{-9}	3×10^{-11}
Leakage with Rowe (1998) DC Eq. (lphd)	≤ 5.3	< 0.2	0.001
Leakage with Rowe (1998) wrinkle Equ. (lphd)	8,700	160 -13,200	60 -16,200
Leakage with Darcy Equation, MGCL alone (lphd)	14,400	700	1,300
Hydraulic conductivity of MGCL, k_{GCL} (m/s)	5×10^{-11}	5×10^{-11}	5×10^{-11}
Leakage with Rowe (1998) wrinkle Equ. (lphd)	7,800	67	36

¹ Submerged and about 0.3 m cover soil; ² About 1 m cover soil; ³ MSW Landfill about 0.3 m gravel drainage layer.

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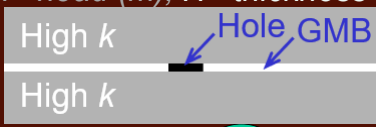
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Holed wrinkle length, L_w (no ELLS) (m)	530	530	530
Holed wrinkle average width, $2b$ (m)	0.2	0.15	0.1
Leakage from Bernoulli's Eq. Q (lphd)	51,000	8,900	10,300
Liner thickness, CCL, H_{GCL} (m)	0.6	0.6	0.6
Hydraulic conductivity below wrinkle, k_{CCL} (m/s)	1×10^{-9}	1×10^{-8}	2×10^{-10}
GMB/GCL interface transmissivity, θ_{CCL} (m ² /s)	1×10^{-6}	1×10^{-7}	2×10^{-9}
Leakage with Darcy Equation, CCL alone (lphd)	8,000	11,000	230
Leakage with Rowe (1998) DC Eq. (lphd)	560	3.6	0.09
Leakage with Rowe (1998) wrinkle Equ. (lphd)	21,000	3,000	60

¹ Submerged and about 0.3 m cover soil; ² About 1 m cover soil; ³ MSW Landfill about 0.3 m gravel drainage layer.

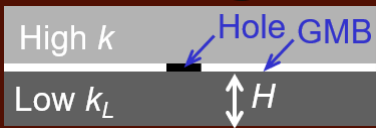
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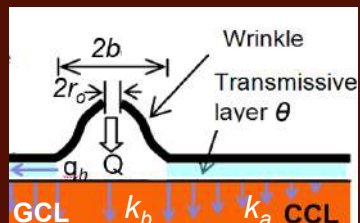
Leakage through a geomembrane defect

- Darcy's law $Q = A k h / H$ $A = \text{area (m}^2\text{)}$, $h = \text{head (m)}$, $H = \text{thickness (m)}$
- Bernoulli's equation $a = \text{area of hole (m}^2\text{)}$
 $Q = 2.6 a \sqrt{h}$ $h = \text{head (m)}$
 $Q = \text{leakage (m}^3\text{/s)}$



$a = \pi r_o^2$
- Giroud's equation if hole in direct contact
 $Q = C_q [1 + 0.1(h/H)^{0.95}] a^{0.1} h^{0.9} k_L^{0.75}$


- Rowe's equation if hole in a wrinkle
 $Q = L [2b k_b + 2(k_a H \theta)^{0.5}] h / H$



with ELLS

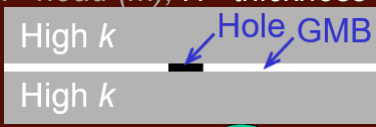
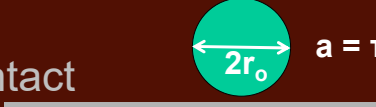
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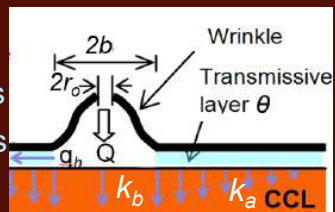
Example liner parameters	$\sigma_{va} < 5 \text{ kPa}$ <i>Pond</i> ¹	$\sigma_{va} \sim 15 \text{ kPa}$ <i>Cover</i> ²	$\sigma_{va} \geq 150 \text{ kPa}$ <i>bottom liner</i> ³
Head on liner, h (m)	5	0.15	0.2
Hole area, a (mm ²)	100	100	100
Holed wrinkle length, L_w (with ELLS) (m)	430	430	430
Holed wrinkle average width, $2b$ (m)	0.2	0.15	0.1
Leakage from Bernoulli's Eq. Q (lphd)	51,000	8,900	10,300
Liner thickness, GCL, H_{GCL} (m)	0.015	0.01	0.007
Hydraulic conductivity below wrinkle, k_{bGCL} (m/s)	2×10^{-10}	6×10^{-8} to 2×10^{-10}	6×10^{-8} to 2×10^{-10}
Hydraulic conductivity below wrinkle, k_{aGCL} (m/s)	5×10^{-11}	2×10^{-10}	3×10^{-11}
GMB/GCL interface transmissivity, θ_{GCL} (m ² /s)	1×10^{-8}	3×10^{-9}	3×10^{-11}
Leakage with Rowe (1998) direct Equation (lphd)	≤ 5.3	< 0.2	0.001
Leakage with Rowe (1998) wrinkle Equ. (lphd)	7,100	130 -10,800	50 -13,100

¹ Submerged and about 0.3 m cover soil; ² About 1 m cover soil; ³ MSW Landfill about 0.3 m gravel drainage layer.

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Leakage through a geomembrane defect

- Darcy's law $Q = A k h/H$ $A = \text{area (m}^2\text{)}$, $h = \text{head (m)}$, $H = \text{thickness (m)}$
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$a = \pi r_o^2$
- Rowe's equation if hole in a wrinkle
 $Q = L [2b k_b + 2(k_a H \theta)^{0.5}] h / H$
 Typical for MSW bottom liners $0.1 \leq 2b \leq 0.2 \text{ m}$
 $0.007 \leq H_{GCL} \leq 0.01 \text{ m}$ $6 \times 10^{-12} \leq \theta_{GCL} \leq 8 \times 10^{-11} \text{ m}^2\text{/s}$
 $0.6 \leq H_{CCL} \leq 1.2 \text{ m}$ $1 \times 10^{-7} \leq \theta_{CCL} \leq 3 \times 10^{-9} \text{ m}^2\text{/s}$
 $2 \times 10^{-10} \leq k_{bGCL} \leq 5 \times 10^{-10} \text{ m/s}$ $3 \times 10^{-11} \leq k_{aGCL} \leq 6 \times 10^{-11} \text{ m/s}$
 $1 \times 10^{-9} \leq k_{bCCL} \leq 5 \times 10^{-10} \text{ m/s}$ $8 \times 10^{-10} \leq k_{bCCL} \leq 3 \times 10^{-10} \text{ m/s}$


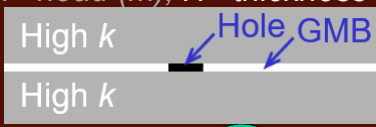
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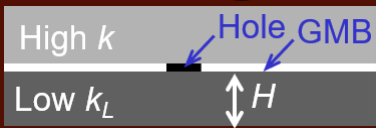
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Leakage through a geomembrane defect

1. Darcy's law $Q = A k h / H$ $A = \text{area (m}^2\text{)}$, $h = \text{head (m)}$, $H = \text{thickness (m)}$
2. Bernoulli's equation $a = \text{area of hole (m}^2\text{)}$
 $Q = 2.6 a \sqrt{h}$ $h = \text{head (m)}$
 $Q = \text{leakage (m}^3\text{/s)}$



Hole GMB
4. Giroud's equation if hole in direct contact
 $Q = C_q [1 + 0.1(h/H)^{0.95}] a^{0.1} h^{0.9} k_L^{0.75}$




Hole GMB

High k

Low k_L

H
5. Rowe's equation if hole in a wrinkle
 $Q = L [2b k_L + 2(k_L H \theta)^{0.5}] h / H$




Hole GMB

High k

Low k_L

T
6. Rowe and Booker (2000)
 $Q = \{4 + [2.455 + 0.685 \tanh(0.6 \ln(r_o/T))] r_o/T\} r_o k_L h$



Hole GMB

High k

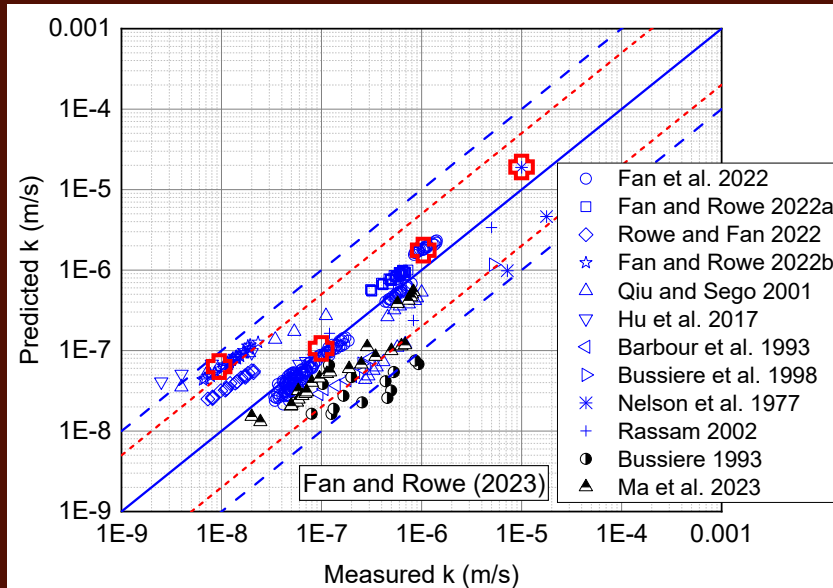
High k

$2r_o$

$a = \pi r_o^2$

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Permeability of tailings



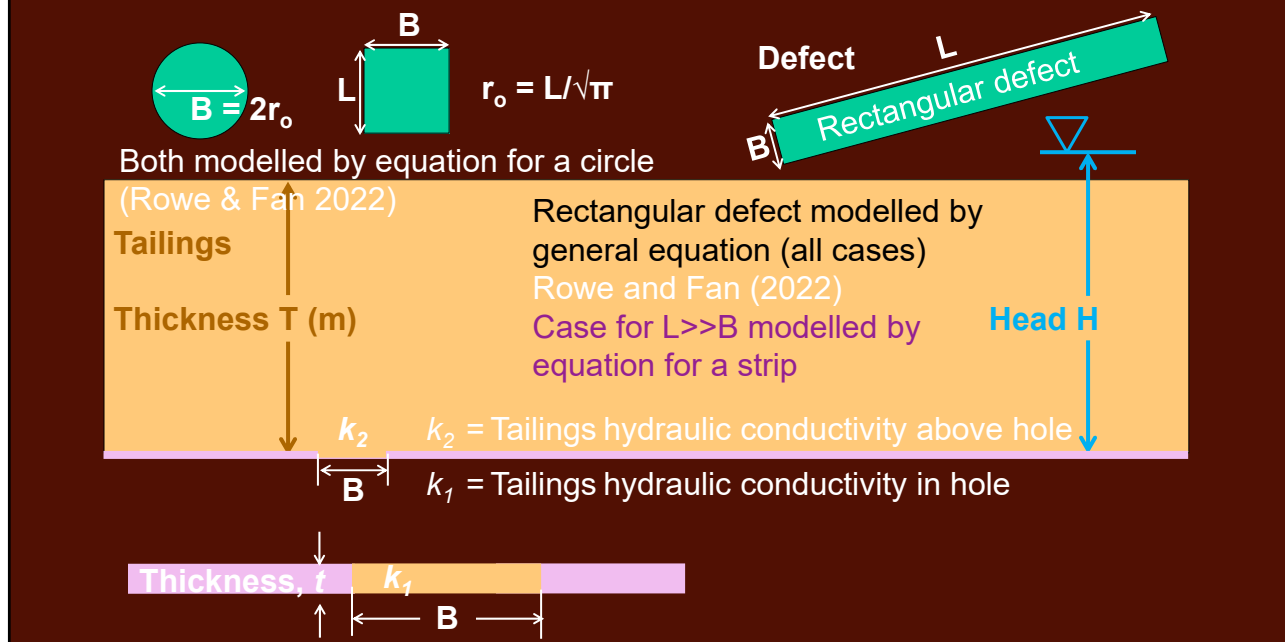
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Leakage through a geomembrane defect in TSF

Head on liner, h (m)	50	50	50	50	50	50
Tailings thickness, H (m)	48	48	48	48	48	48
Hole area, a (mm ²)	100	100	100	100	100	100
Hydraulic conductivity of tailings at hole, k_T (m/s)	0	1×10^{-4}	1×10^{-5}	1×10^{-6}	1×10^{-7}	1×10^{-8}
Leakage from Rowe-Booker Eq. (2000) (lphd)	162,000	9,750	975	97.5	9.75	0.975
Leakage from Rowe-Fan Eq. (2022a) (lphd)	162,000	6,720	672	67.2	6.7	0.67
Head on liner, h (m)	50	100	150	200	250	300
Tailings thickness, H (m)	48	98	148	198	248	298
Hole area, a (mm ²)	100	100	100	100	100	100
Hydraulic conductivity of tailings at hole, k_T (m/s)	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}
Leakage from Rowe-Booker Eq. (2000) (lphd)	97.5	195	292	390	487	585
Leakage from Rowe-Fan Eq. (2022) (lphd)	67.2	134	202	269	512	745

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6. Rowe and Fan (2022b) General solution for leak below tailings



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Leakage through a geomembrane defect in TSF

Head on liner, h (m)	50	50	50	50	50	50
Tailings thickness, H (m)	48	48	48	48	48	48
Hole area, a (mm ²)	100	100	100	10,000	10,000	10,000
Hole length (m)	0.01	0.1	1	0.1	1	10
Hole width (m)	0.01	0.001	0.0001	0.1	0.01	0.001
Hydraulic conductivity of tailings at hole, k_T (m/s)	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}
Leakage from Rowe-Fan Eq. (2022b) (lphd)	71	98	164	1,020	1,670	6,580
Head on liner, h (m)	50	50	50	50	300	300
Tailings thickness, H (m)	48	48	48	48	298	298
Hole area, a (mm ²)	100,000	100,000	100,000	100,000	100,000	100,000
Hole length (m)	0.316	0.1	0.01	0.001	0.316	0.001
Hole width (m)	0.316	1	10	100	100,000	100
Hydraulic conductivity of tailings at hole, k_T (m/s)	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}	1×10^{-6}
Leakage from Rowe-Fan Eq. (2022b) (lphd)	3,330	4,220	12,400	72,100	19,900	327,000

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Take home message

There are many (all simple) equations – **BUT**
You need to understand which equation is most
suitable for your situation

A barrier system design **that does not properly
calculate and consider the potential consequence of
leakage** is not a design; it is wishful thinking

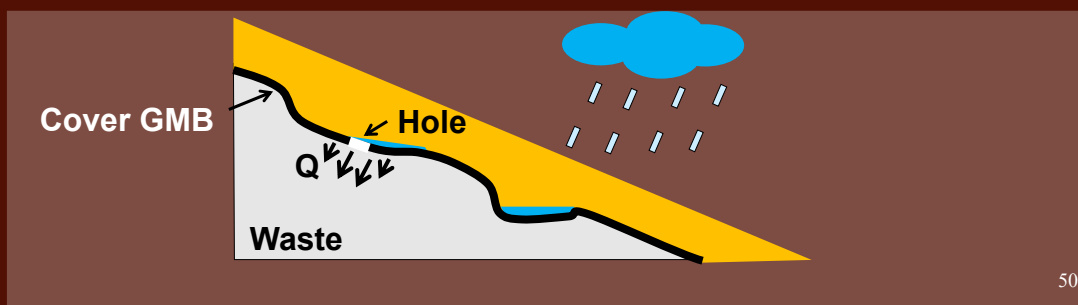
Do not destroy composite liner action
in a wrong-headed attempt to solve another problem

[5:00]

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Compared to base liners, GMB strains and leakage for covers may additionally depend on:

1. Weather
2. Differential settlement
3. Slope
4. Wrinkles on slopes
5. Cover soil properties



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Take home messages

- Differential can substantially increase leakage on 4H:1V slopes.
- Care is needed when filling zones of differential settlement not to aggravate the problem.

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<p>Short Course on GEOMEMBRANES AND COMPOSITE LINERS IN LANDFILLS AND MINING: MOVING FORWARD</p>	<p>Sunday 17 Sept. 2023</p>	
<p>2. Leakage through liners</p> <p>R. Kerry Rowe OC, FRS, FREng, NAE Barrington Batchelor Distinguished University Professor and Canada Research Chair in Geotechnical and Geoenvironmental Engineering</p>		
 <p>at Queen's-RMC</p>	<p>Queen's University Kingston Canada www.geoeng.ca</p>	 

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